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# A full-potential linear-muffin-tin-orbital molecular-dynamics study on the distorted cage structures of Si<sub>60</sub> and Ge<sub>60</sub> clusters

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**Abstract.** Using a full-potential linear-muffin-tin-orbital molecular-dynamics (FP-LMTO-MD) method, we have performed calculations on the structures and the binding energies of  $Si_{60}$  and  $Ge_{60}$  clusters. The results calculated suggest that the stable structures for  $Si_{60}$  and  $Ge_{60}$  clusters are both distorted truncated icosahedra, with  $T_h$  symmetry. Their fullerene cage structures remain, but they look like puckered balls. Four distinct Si–Si bond lengths in  $Si_{60}$ , three distinct Ge–Ge bond lengths in  $Ge_{60}$ , and lower  $T_h$  symmetry make the two structures different from that with  $I_h$  symmetry and two C–C bond lengths in  $C_{60}$ .

#### 1. Introduction

Studies on the structures and electronic and chemical properties of  $C_n$  [1–6],  $Si_n$  [7–12], and  $Ge_n$  [13–17] clusters have produced a wealth of exciting information about their potential applications. Their fullerene structures have attracted considerable attention. The existence of the fullerenes as a family for C and Si clusters has become established; among the various structures, the  $C_{60}$  cage is the most fascinating. The structure of  $C_{60}$  is a truncated icosahedron with I<sub>h</sub> symmetry, containing 20 hexagons and 12 pentagons on its almost spherical surface. Silicon and germanium are the heavier homologues in the periodic table. We may expect Si<sub>60</sub> and Ge<sub>60</sub> also to have cage structures and interesting properties.

Up to now, a few reports [18–25] have involved  $Si_{60}$  structure, but the results are controversial. The authors of references [20–23] have proposed that  $Si_{60}$  still exhibits the same buckminsterfullerene structure (I<sub>h</sub> symmetry) as  $C_{60}$ , using a double-zeta (DZ) basis set with *ab initio* effective-core potentials (ECP) on silicon atoms or the Austin model 1 method. Their calculated results suggest that the perfect cage structure represents a minimum of the potential energy surface, which is much more favourable than a stacked naphthalene structure or a cylindrical structure. But, using a conventional orthogonal tight-binding molecular dynamics [24], Khan and Broughton have found that the icosahedral cage structure of  $Si_{60}$  is not stable and relaxes into a structure resembling a puckered ball. By the same method, Menon and Subbaswamy found that the perfect icosahedral cage is unstable, distorting to a lower-symmetry  $C_{2h}$  structure with no change in the threefold coordination [25]. They proposed that a  $Si_{60}$  network is more stable than a  $Si_{60}$  fullerene with  $C_{2h}$  symmetry, but for  $C_{60}$  clusters, the former is less favourable than the latter.

Experimental results are also controversial. A saturation study of  $Si_{60}$  positive ions shows that the average number of ammonia molecules absorbed rapidly is close to 6 [26]. This

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may imply the fullerene structure [27]. However, fragmentation analysis of  $Si_{60}$  positive ions supports the hypothesis of a stacked naphthalene-like structure [28].

Germanium is contiguous to silicon in the periodic table. A few reports have involved their similarities [14, 15, 29, 30]. Photofragmentation and reactivity results obtained in some of the semiconductor cluster experiments [31, 32] gave evidence that the structures of silicon and germanium clusters may be much the same. For the larger clusters,  $Si_{60}$  and  $Ge_{60}$ , is there still this similarity between them in structure? Nagase investigated the structure of  $Ge_{60}$  [22]. Nagase also proposed that the perfect cage structure is the structure of  $Ge_{60}$ . But, the authors of reference [25] concluded that, among the group IV elements, perfect icosahedral symmetry is unique to carbon. In the hope of obtaining more accurate structures and establishing the similarities of and differences between the two clusters, we employ a more sophisticated method to investigate  $Si_{60}$  and  $Ge_{60}$ . The aim in this paper is to find the structure of  $Si_{60}$  and  $Ge_{60}$  corresponding to the most important buckminsterfullerene structure (I<sub>h</sub> symmetry) of  $C_{60}$ , and then to make a comparison between them. Our calculated results reveal that the corresponding structures of  $Si_{60}$  and  $Ge_{60}$  clusters are both distorted cage structures, with the same symmetry  $T_h$ , but  $Ge_{60}$  is slightly less distorted than  $Si_{60}$ .

### 2. Method

The FP-LMTO method [35–39] is a self-consistent implementation of the Kohn–Sham equations in the local-density approximation [33]. This method expands the electron wave functions in terms of muffin-tin orbitals [34]. Also, this method uses a completely general form for the potential and density in which space is divided into non-overlapping muffin-tin spheres and the remaining interstitial region (in which the potential is expressed as a linear combination of Hankel functions), instead of the atomic sphere approximation (ASA). The details of how the molecular-dynamics simulation can be performed are given in references [35, 36].

### 3. Structures and discussion

The perfect truncated icosahedron of C<sub>60</sub> is a very stable cage structure, in which each atom is bonded to three other atoms and there are two distinct bond lengths: six-six ring fusion and five-six ring fusion. The fullerene cage is the most important structure among all of the isomers of the C<sub>60</sub> cluster. We wondered whether the heavier homologues Si and Ge would also form the same stable icosahedral cage structures as the C<sub>60</sub> cluster. Starting with perfect icosahedral configurations in proportion to that of  $C_{60}$ , we have performed calculations on Si<sub>60</sub> and Ge<sub>60</sub> clusters by using the full-potential linear-muffin-tin-orbital molecular-dynamics (FP-LMTO-MD) method. In the process of optimization, no restrictions are imposed. The process is stopped when the condition of self-consistency is met. We find that the initial perfect icosahedral configurations with I<sub>h</sub> symmetry for Si and Ge are both unstable, distorting to a geometry with lower T<sub>h</sub> symmetry but the same coordination. We present the three cage structures of the C<sub>60</sub>, Si<sub>60</sub>, and Ge<sub>60</sub> clusters in figure 1, from left to right. Two-dimensional perspective views of two of them (Si<sub>60</sub> on the left and Ge<sub>60</sub> on the right) are shown in figure 2, and their point groups, bond lengths, and binding energies are given in table 1. It is obvious that their cage structures have become seriously deformed, like puckered balls, in which three polygons (a pentagon and two hexagons) have been distorted. The included angles between the edges of the polygons have obviously changed. The root mean square deviations  $\delta\theta$  of the included angles relative to those of the perfect cage are given in table 2.

The data suggest that  $Ge_{60}$  does indeed resemble  $Si_{60}$  in structure. However, it is found



Figure 1. The final configurations of the molecular-dynamics optimization for  $Si_{60}$  and  $Ge_{60}$ . The distorted structures have  $T_h$  symmetry. The structures shown are those of, from left to right,  $C_{60}$ ,  $Si_{60}$ , and  $Ge_{60}$ .



**Figure 2.** Two-dimensional perspective views of Si<sub>60</sub> (on the left) and Ge<sub>60</sub> (on the right). *a*, *b*, *c*, and *d* represent the four different bond lengths of Si<sub>60</sub>. There are only three bond lengths, *a*, *b*, and *c*, in the Ge<sub>60</sub> cluster.

**Table 1.** The point groups, bond lengths (a, b, c, d (Å)), and binding energies (eV/atom) for Si<sub>60</sub> and Ge<sub>60</sub> clusters.

Cluster	Point group	а	b	с	d	Binding energy
Si <sub>60</sub>	T <sub>h</sub>	2.218	2.271	2.280	2.295	4.899
Ge <sub>60</sub>	T <sub>h</sub>	2.364	2.434	2.449		3.226

that all three values of  $\delta\theta$  for Ge<sub>60</sub> are less than those of Si<sub>60</sub>, as given in table 2. In addition, all the five edge lengths of the pentagons in Ge<sub>60</sub> are equal, but this is not so for Si<sub>60</sub>. Ge<sub>60</sub> seems to be slightly less distorted than Si<sub>60</sub>. Despite their distortion, they both still have high symmetry, T<sub>h</sub>. There are four bond lengths, with average 2.279 Å, ranging from 2.218 Å to 2.295 Å for the Si<sub>60</sub> cluster. But Ge<sub>60</sub> has only three bond lengths. Its average bond length is 2.439 Å, situated between the minimum 2.364 Å and the maximum 2.449 Å. Obviously, our structures are different from the perfect cage structures reported previously in references [18–23]. Despite

**Table 2.** Root mean square deviations  $\delta\theta$  (deg) of the included angles in the three polygons relative to those of the perfect cage.  $\delta\theta_1$  refers to that of the pentagon,  $\delta\theta_2$  and  $\delta\theta_3$  to those of the two hexagons.

Cluster	$\delta \theta_1$	$\delta \theta_2$	$\delta \theta_3$
Si <sub>60</sub>	9.93	8.80	18.62
Ge <sub>60</sub>	8.16	8.76	16.43

the structure of Si<sub>60</sub> found in this work being similar to that—resembling a puckered ball reported by Khan, Menon [24, 25], our result is different from theirs. Firstly, the structure obtained by us has a different symmetry from theirs, although these structures have all distorted into lower-symmetry forms. Our structure has  $T_h$  symmetry, while Si<sub>60</sub> has  $C_{2h}$  symmetry in reference [25]. Secondly, there are four distinct bond lengths in our structure, but all of the bonds are approximately of length 2.37 Å in reference [24]. For the Ge<sub>60</sub> cluster, to our knowledge, the structure like a puckered ball, with  $T_h$  symmetry, is reported for the first time here. Our calculations suggest that the structures of Si<sub>60</sub> and Ge<sub>60</sub> are about the same. But there are some slight differences between them: four distinct bond lengths in Si<sub>60</sub> and three distinct bond lengths in Ge<sub>60</sub>; and different included-angle changes for the polygons.

#### 4. Summary

Using a full-potential linear-muffin-tin-orbital molecular-dynamics (FP-LMTO-MD) method, we have performed calculations on the structures of the large clusters  $Si_{60}$  and  $Ge_{60}$  corresponding to the fullerene cage structure of the  $C_{60}$  cluster. The calculated results suggest that the corresponding stable structures of the clusters  $Si_{60}$  and  $Ge_{60}$  are both distorted icosahedral cages resembling puckered balls, with  $T_h$  symmetry.  $Ge_{60}$  is slightly less distorted than  $Si_{60}$  in structure. There are four different bond lengths in  $Si_{60}$ , but only three for the  $Ge_{60}$  cluster.

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#### References

- [1] Kroto H W, Allaf A W and Balm S P 1991 Chem. Rev. 91 1213
- [2] Phillips J C 1985 J. Chem. Phys. 83 3330
- [3] Elkind J L, Alford J M, Weiss F D, Laaksonen R T and Smalley R E 1987 J. Chem. Phys. 87 2397
- [4] Jarrold M F and Honea E C 1991 J. Phys. Chem. 95 9181
- [5] Diederich F and Whetten R L 1991 Angew. Chem. Int. Edn Engl. 30 678
- [6] Fuke K, Tsukamoto K, Misaizu F and Sanekata M 1993 J. Chem. Phys. 99 7807
- [7] Jarrold M F 1991 Science 252 1085
- [8] Grossman J C and Mitas L 1995 Phys. Rev. B 52 16735
- [9] Bahel A and Ramakrishna M V 1994 Phys. Rev. B 51 13 849
- [10] Kaxiras E 1989 Chem. Phys. Lett. 163 323
- [11] Ray U and Jarrold M F 1991 J. Chem. Phys. 94 2631
- [12] Raghavachari K 1988 J. Chem. Phys. 89 2219
- [13] Archibong E F and St-Amant A 1998 J. Chem. Phys. 109 962
- [14] Dixon D A and Gole J L 1992 Chem. Phys. Lett. 188 560
- [15] Dai D and Balasubramanian K 1992 J. Chem. Phys. 96 8345
- [16] Dai D, Sumathi K and Balasubramanian K 1992 Chem. Phys. Lett. 193 251

- [17] Dai D and Balasubramanian K 1996 J. Chem. Phys. 105 5901
- [18] Piqueras M C, Crespo R, Orti E and Tomas F 1993 Synth. Met. 61 155
- [19] Crespo R, Piqueras M C and Tomas F 1996 Synth. Met. 77 13
- [20] Piqueras M C, Crespo R, Orti E and Tomas F 1993 Chem. Phys. Lett. 213 509
- [21] Nagase S and Kobayashi K 1991 Chem. Phys. Lett. 187 291
- [22] Nagase S 1993 Pure Appl. Chem. 65 675
- [23] Slanina Z, Lee S L, Kobayashi K and Nagase S 1994 J. Mol. Struct. (Theochem.) 312 175
- [24] Khan F S and Broughton J Q 1991 Phys. Rev. B 43 11754
- [25] Menon M and Subbaswamy K R 1994 Chem. Phys. Lett. 219 219
- [26] Jarrold M F, Ijiri Y and Ray U 1991 J. Chem. Phys. 94 3607
- [27] Hirsch A, Li Q and Wudl F 1991 Angew. Chem. Int. Edn Engl. 30 1309
- [28] Jelski D A, Wu Z C and George T F 1990 J. Cluster Sci. 1 143
- [29] Pacchioni G and Koutecky J 1986 J. Chem. Phys. 84 3301
- [30] Andzelm J, Russo N and Salahub D R 1987 J. Chem. Phys. 87 6562
- [31] Alford J M, Laaksonen R T and Smalley R E 1991 J. Chem. Phys. 94 2618
- [32] Zhang Q L, Liu Y, Curl R F, Tittel F K and Smalley R E 1988 J. Chem. Phys. 88 1670
- [33] Kohn W and Sham L J 1965 Phys. Rev. 140 A1133
- [34] Andersen O K 1975 Phys. Rev. B 12 3060
- [35] Methfessel M and Schilfgaarde M V 1993 Int. J. Mod. Phys. B 7 262
- [36] Methfessel M and Schilfgaarde M V 1993 Phys. Rev. B 48 4937
- [37] Methfessel M 1988 Phys. Rev. B 38 1537
- [38] Methfessel M, Rodriguez C O and Andersen O K 1989 Phys. Rev. B 40 2009
- [39] Qiu M, Jiang M, Zhao Y J and Cao P L 1999 J. Chem. Phys. 110 10738